Paper Id:

Roll No:

B. TECH. (SEM III) THEORY EXAMINATION 2019-20 DISCRETE STRUCTURES & THEORY OF LOGIC

Time: 3 Hours Total Marks: 100

Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

Attempt all questions in brief. 1.

110323

 $2 \times 10 = 20$

Sub Code:KCS303

Qno.	Question	Marks	CO
a.	Define various types of functions.	2	COI
b.	How many symmetric and reflexive relations are possible from a set A containing 'n' elements?	2	COI
c.	Let Z be the group of integers with binary operation * defined by $a*b=a+b-2$, for all $a,b\in Z$. Find the identity element of the group $\langle Z,*\rangle$	2	CO2
d.	Show that every cyclic group is abelian.	2	CO2
e.	Prove that a lattice with 5 elements is not a boolean algebra.	2	CO3
f.	Write the contra positive of the implication: "if it is Sunday then it is a holiday".	2	CO4
g.	Show that the propositions $p \rightarrow q$ and $\neg p \lor q$ are logically equivalent.	2	CO4
h.	Show that there does not exist a graph with 5 vertices with degrees 1, 3, 4, 2, 3 respectively.	2	CO5
i.	Obtain the generating function for the sequence 4, 4, 4, 4, 4, 4, 4	2	CO5
j.	Define Pigeon hole principle.	2	CO5

SECTION B

2. Attempt any three of the following:

 $3 \times 10 = 30$

	Accompt any times of the following.	JAIU	30
Qno.	Question	Marks	CO
a.	Prove that $\frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \dots + \frac{1}{\sqrt{n}} > \sqrt{n}$ for $n \ge 2$ using principle	10	CO1
<u></u>	of mathematical induction	10	CO2
b.	What do you mean by cosets of a subgroup? Consider the group Z of integers under addition and the subgroup.	10	CO2
	$H = \{, -12, -6, 0, 6 \ 12,\}$ considering of multiple of 6		
	(i) Find the cosets of H in Z		
	(ii) What is the index of H in Z.		
c.	Show that the following are equivalent in a Boolean algebra $a \le b \Leftrightarrow a * b' = 0 \Leftrightarrow b' \le a' \Leftrightarrow a' \oplus b = 1$	10	CO3
d.	Show that $((P \lor Q) \land \neg (\neg Q \lor \neg R)) \lor (\neg P \lor \neg Q) \lor (\neg P \lor \neg R)$ is a	10	CO4
	tautology by using equivalences.		
e.	Define planar graph. Prove that for any connected planar graph,	10	CO5
	v - e + r = 2 Where v, e, r is the number of vertices, edges, and regions of		
	the graph respectively.		

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SECTION C

3. Attempt any one part of the following:

 $1 \times 10 = 10$

Qno.	Question	Marks	CO
a.	Find the numbers between 1 to 500 that are not divisible by any of the	10	CO1
	integers 2 or 3 or 5 or 7.		
b.	Is the "divides" relation on the set of positive integers transitive? What is	10	CO1
	the reflexive and symmetric closure of the relation?		
	$R = \{(a, b) \mid a > b\}$ on the set of positive integers?		

4. Attempt any one part of the following:

 $1 \times 10 = 10$

Qno.	Question	Marks	СО
a.	What is Ring? Define elementary properties of Ring with example.	10	CO2
b.	Prove or disprove that intersection of two normal subgroups of a group G is again a normal subgroup of G.	10	CO2

5. Attempt any one part of the following:

 $1 \times 10 = 10$

Qno.	Question	Marks	CO
a.	Let (L, \vee, \wedge, \leq) be a distributive lattice and $a, b \in L$ if $a \wedge b = a \wedge c$ and	10	CO3
	$a \lor b = a \lor c$ then show that $b = c$		
b.	Obtain the principle disjunctive and conjunctive normal forms of the	10	CO3
	formula $(\Box p \rightarrow r) \land (q \leftrightarrow p)$		

6. Attempt any one part of the following:

 $1 \times 10 = 10$

Qno.	Question	Marks	CO
a.	Explain various Rules of Inference for Propositional Logic.	10	CO4
b.	Prove the validity of the following argument "if the races are fixed so the	10	CO4
	casinos are crooked, then the tourist trade will decline. If the fourist trade		
	decreases, then the police will be happy. The police force is never happy.		
	Therefore, the races are not fixed.		

7. Attempt any one part of the following:

 $1 \times 10 = 10$

Qno.	Question	Marks	CO
a.	Solve the following recurrence equation using generating function	10	CO5
	G(K) - 7G(K-1) + 10G(K-2) = 8K + 6		
b.	A collection of 10 electric bulbs contain 3 defective ones	10	CO5
	(i) In how many ways can a sample of four bulbs be selected?		
	(ii) In how many ways can a sample of 4 bulbs be selected which contain		
	2 good bulbs and 2 defective ones?		
	(iii) In how many ways can a sample of 4 bulbs be selected so that either		
	the sample contains 3 good ones and 1 defectives ones or 1 good and 3		
	defectives ones?		